

# Package: mqqcause (via r-universe)

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**Type** Package

**Title** Multivariate Quantile-on-Quantile Granger Causality

**Version** 1.0.0

**Description** Implements bivariate and Multivariate Quantile-on-Quantile Granger causality tests building on the Quantile-on-Quantile regression framework of Sim and Zhou (2015) [doi:10.1016/j.jbankfin.2015.01.013](https://doi.org/10.1016/j.jbankfin.2015.01.013) and the quantile Granger causality test of Troster (2018) [doi:10.1080/07474938.2016.1172400](https://doi.org/10.1080/07474938.2016.1172400). The bivariate test estimates the local-linear slope in the quantile regression of  $y_t$  on lagged  $x_t$  with lagged  $y_t$  as control, using Gaussian kernel weights, and tests it against zero by paired bootstrap. The multivariate (conditional) test additionally conditions on a set of moderators  $Z$  and optional  $x$  times  $Z$  interaction terms, in the spirit of Sinha, Ghosh, Hussain, Nguyen and Das (2023) [doi:10.1016/j.eneco.2023.107021](https://doi.org/10.1016/j.eneco.2023.107021). A Sup-Wald summary across the quantile grid is also provided. Heatmaps and 3D surfaces default to the 'MATLAB' 'Parula' colour map.

**License** GPL-3

**Encoding** UTF-8

**RoxygenNote** 7.3.1

**Depends** R (>= 3.5.0)

**Imports** quantreg (>= 5.0), plotly (>= 4.0.0), stats, utils, grDevices

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0)

**URL** <https://github.com/merwanroudane/qqcaus>

**BugReports** <https://github.com/merwanroudane/qqcaus/issues>

**Config/testthat/edition** 3

**NeedsCompilation** no

**Config/pak/sysreqs** cmake make libicu-dev libuv1-dev libssl-dev

**Repository** <https://merwanroudane.r-universe.dev>

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mqqcause-package	<i>mqqcause: Multivariate Quantile-on-Quantile Granger Causality</i>
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## Description

Implements bivariate Quantile-on-Quantile Granger causality and the multivariate (conditional) version with a vector of moderators and optional interaction terms. A Sup-Wald summary across the (theta, tau) grid is also provided (Troster, 2018).

## Author(s)

Dr Merwan Roudane <[merwanroudane920@gmail.com](mailto:merwanroudane920@gmail.com)>  
 GitHub: <https://github.com/merwanroudane/qqcaus>

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parula_colors	<i>MATLAB-style colour palettes for mqqcause</i>
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## Description

Colour palettes used by mqqcause plotting functions. The default scale is MATLAB Parula.

## Usage

```
parula_colors(n = 256)
matlab_jet_colors(n = 256)
turbo_colors(n = 256)
bluered_colors(n = 256)
sinha_colors(n = 256)
mqqcause_palette(cols, n_breaks = 32)
resolve_colorscale(name = "Parula", n_breaks = 32)
mqqcause_colorscales(show_preview = TRUE)
```

**Arguments**

n	Number of colours.
cols	Character vector of hex colours.
n_breaks	Stops for the plotly list.
name	Scale name (Parula by default).
show_preview	Print descriptions.

**Value**

Character vector or list.

**Examples**

```
parula_colors(8)
matlab_jet_colors(8)
turbo_colors(8)
bluered_colors(8)
sinha_colors(8)
mqqcause_colorscales(show_preview = FALSE)
```

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plot\_qq\_causality\_3d *Visualisations for QQ Causality Results*

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**Description**

3D surface, heatmap, contour and significance-only heatmap visualisations of QQ Granger-causality results, defaulting to MATLAB Parula.

**Usage**

```
plot_qq_causality_3d(qq_result, value = "t_value",
                    colorscale = "Parula", show_contour = TRUE,
                    x_label = "X Quantile (tau)",
                    y_label = "Y Quantile (theta)", title = NULL)

plot_qq_causality_heatmap(qq_result, value = "t_value",
                          colorscale = "Parula", show_stars = TRUE,
                          x_label = "X Quantile (tau)",
                          y_label = "Y Quantile (theta)", title = NULL)

plot_qq_causality_contour(qq_result, value = "t_value",
                           colorscale = "Parula",
                           x_label = "X Quantile (tau)",
                           y_label = "Y Quantile (theta)", title = NULL)

plot_significance_heatmap(qq_result, colorscale = "Parula")
```

**Arguments**

qq\_result      A qq\_causality or mqq\_causality object.  
 value          Column to plot.  
 colorscale     Default "Parula".  
 show\_contour, show\_stars, x\_label, y\_label, title  
                  Plot options.

**Value**

A plotly object.

**Examples**

```
## Small toy example -- auto-tested.
set.seed(1); n <- 80
x <- rnorm(n); y <- 0.3 * c(0, x[-n]) + rnorm(n, sd = 0.4)
fit <- qq_causality(x, y,
  y_quantiles = c(0.25, 0.5, 0.75),
  x_quantiles = c(0.25, 0.5, 0.75),
  n_boot = 10, verbose = FALSE)
p1 <- plot_qq_causality_heatmap(fit, value = "t_value", show_stars = TRUE)
p2 <- plot_qq_causality_3d(fit, value = "t_value")
p3 <- plot_qq_causality_contour(fit, value = "t_value")
p4 <- plot_significance_heatmap(fit)
```

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 qq\_causality

*Quantile-on-Quantile Granger Causality (Bivariate and Multivariate)*


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**Description**

Tests whether the tau-quantile of  $x_{t-1}$  Granger-causes the theta-quantile of  $y_t$ . The multivariate variant conditions on a set of moderators  $Z$  and optional  $x \cdot Z$  interaction terms (the conditional-causality test that under-pins Sinha et al., 2024).

**Usage**

```
qq_causality(x, y,
  y_quantiles = seq(0.05, 0.95, by = 0.05),
  x_quantiles = seq(0.05, 0.95, by = 0.05),
  bandwidth = 0.05, n_boot = 200,
  cdf_based_kernel = TRUE,
  cause_name = "X", effect_name = "Y",
  verbose = TRUE, seed = 42)

mqq_causality(x, y, moderators = list(),
  y_quantiles = seq(0.05, 0.95, by = 0.05),
  x_quantiles = seq(0.05, 0.95, by = 0.05),
```

```
bandwidth = 0.05, n_boot = 200, interactions = TRUE,
cdf_based_kernel = TRUE,
cause_name = "X", effect_name = "Y",
verbose = TRUE, seed = 42)
```

```
sup_wald(qq_result, alpha = 0.05)
qq_causality_to_matrix(qq_result, value = "t_value")
```

### Arguments

x, y	Numeric vectors (cause and effect).
moderators	Named list of numeric vectors (the conditioning set Z).
y_quantiles, x_quantiles	Numeric vectors of quantile levels in (0, 1).
bandwidth	Kernel bandwidth on the empirical-CDF scale.
n_boot	Bootstrap replicates.
interactions	Include x*Z cross-terms (mqq_causality).
cdf_based_kernel	Use CDF-distance kernel.
cause_name, effect_name	Variable names for printing.
verbose	Print progress.
seed	RNG seed.
qq_result	A qq_causality / mqq_causality object.
value	Column to pivot.
alpha	Significance threshold.

### Value

For qq\_causality and mqq\_causality, an object of class "qq\_causality" or "mqq\_causality".  
sup\_wald returns a list; qq\_causality\_to\_matrix returns a numeric matrix.

### References

Sim, N., Zhou, H. (2015). *Journal of Banking and Finance*, 55, 1-12.  
Troster, V. (2018). Testing for Granger-causality in Quantiles. *Econometric Reviews*, 37(8), 850-866.

### Examples

```
set.seed(1); n <- 200
x <- rnorm(n); z <- rnorm(n)
y <- 0.3 * c(0, x[-n]) + 0.2 * c(0, z[-n]) + rnorm(n, sd = 0.4)
fit <- mqq_causality(x, y, list(Z = z),
                    y_quantiles = c(0.25, 0.5, 0.75),
                    x_quantiles = c(0.25, 0.5, 0.75),
```

```

n_boot = 30, verbose = FALSE)
print(fit)
sup_wald(fit)

```

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qq\_weights

*Numerical building blocks*


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### Description

Gaussian kernel, QQ weights, and weighted quantile regression via `quantreg::rq.wfit`. Exposed for advanced users.

### Usage

```

qq_weights(x, tau, h = 0.05, cdf_based = TRUE)
gaussian_kernel(u)
weighted_qr(y, X, tau, weights = NULL)

```

### Arguments

x, y, u	Numeric vectors.
X	Numeric design matrix.
tau	Quantile in (0, 1).
h	Bandwidth.
cdf_based	Use empirical-CDF distance kernel.
weights	Optional numeric weights.

### Value

Numeric vector or list.

### Examples

```

set.seed(1)
x <- rnorm(50)
w <- qq_weights(x, tau = 0.5)
sum(w) # weights sum to length(x)
k <- gaussian_kernel(seq(-3, 3, by = 1))
X <- cbind(1, x)
y <- 0.5 * x + rnorm(50, sd = 0.3)
fit <- weighted_qr(y, X, tau = 0.5, weights = w)
fit$coef

```

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